

Mth102 Final Formula Sheet

Standard deviation: $s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{\sum x^2 - (\sum x)^2/n}{n-1}}$

Mean of a random variable: $\mu = \sum xP(X = x)$

Standard deviation of a random variable: $\sigma = \sqrt{\sum (x - \mu)^2 P(X = x)} = \sqrt{\sum x^2 P(X = x) - \mu^2}$

Binomial probability

$$P(X = x) = \binom{n}{x} p^x (1-p)^{n-x} \quad \mu = np \quad \sigma = \sqrt{np(1-p)}$$

$(1-\alpha)100\%$ CI about μ , σ known: $\bar{x} \pm z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$

$(1-\alpha)100\%$ CI about μ , σ unknown: $\bar{x} \pm t_{\alpha/2} \cdot \frac{s}{\sqrt{n}}$

$(1-\alpha)100\%$ CI about p , $\hat{p} \pm z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

Margin of error about μ : $E = z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$

Sample size necessary: $n = \left(\frac{z_{\alpha/2} \cdot \sigma}{E} \right)^2$

Margin of error about p : $E = z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

$$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}} \quad t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \quad z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$